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## Estimating cotton evapotranspiration crop coefficients with a multispectral vegetation index

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**Abstract** Crop coefficients are a widely used and universally accepted method for estimating the crop evapotranspiration ( $ET_c$ ) component in irrigation scheduling programs. However, uncertainties of generalized basal crop coefficient ( $K_{cb}$ ) curves can contribute to  $ET_c$  estimates that are substantially different from actual  $ET_c$ . Limited research with corn has shown improvements to irrigation scheduling due to better water-use estimation and more appropriate timing of irrigations when  $K_{cb}$  estimates derived from remotely sensed multispectral vegetation indices (VIs) were incorporated into irrigation-scheduling algorithms. The purpose of this article was to develop and evaluate a  $K_{cb}$  estimation model based on observations of the normalized difference vegetation index (NDVI) for a full-season cotton grown in the desert southwestern USA. The  $K_{cb}$  data used in developing the relationship with NDVI were derived from back-calculations of the FAO-56 dual crop coefficient procedures using field data obtained during two cotton experiments conducted during 1990 and 1991 at a site in central Arizona. The estimation model consisted of two regression relations: a linear function of  $K_{cb}$  versus NDVI ( $r^2=0.97$ ,  $n=68$ ) used to estimate  $K_{cb}$  from early vegetative growth to effective full cover, and a multiple regression of  $K_{cb}$  as a function of NDVI and cumulative growing-degree-days (GDD) ( $r^2=0.82$ ,  $n=64$ ) used to estimate  $K_{cb}$  after effective full cover was attained. The NDVI for cotton at effective full cover was  $\sim 0.80$ ; this value was used to mark the point at which the model transferred from the linear to the

multiple regression function. An initial evaluation of the performance of the model was made by incorporating  $K_{cb}$  estimates, based on NDVI measurements and the developed regression functions, within the FAO-56 dual procedures and comparing the estimated  $ET_c$  with field observations from two cotton plots collected during an experiment in central Arizona in 1998. Preliminary results indicate that the  $ET_c$  based on the NDVI- $K_{cb}$  model provided close estimates of actual  $ET_c$ .

### Introduction

A fundamental requirement for accurate irrigation scheduling is the determination of actual crop evapotranspiration ( $ET_c$ ) for each day during the growing period. A practical and extensively applied method for estimating  $ET_c$  is the crop coefficient ( $K_c$ ) approach (Doorenbos and Pruitt 1977; Jensen and Allen 2000), in which an experimentally developed dimensionless  $K_c$  is multiplied by reference evapotranspiration (traditionally grass or alfalfa) to compute  $ET_c$ . Values of  $K_c$  determined for most agricultural crops will typically vary in relation to changes in vegetative growth until effective full cover is attained. After full cover, the  $K_c$  will tend to decline, the extent of which is primarily dependent on the particular growth characteristics of the crop (Jensen et al. 1990) and the irrigation management during the late season (Allen et al. 1998). A crop coefficient curve is the seasonal distribution of  $K_c$ , often expressed as a smooth continuous function in time or some other time-related index, such as thermal units (Jensen et al. 1990).

Increased soil evaporation can cause  $K_c$  values to deviate significantly from the empirically determined  $K_c$  function for several days following irrigation or heavy rainfall. To account for the effects of soil evaporation, the Food and Agriculture Organization (FAO) Irrigation and Drainage paper no. 56 (FAO-56), *Crop evapotranspiration* (Allen et al. 1998), presented dual crop coefficient procedures to allow computation of

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more precise estimates of daily  $ET_c$  for days following irrigation or rain. For the FAO-56 dual crop coefficient approach, the single  $K_c$  is separated into two coefficients, a basal crop coefficient,  $K_{cb}$  (primarily crop transpiration), and a wet soil evaporation coefficient,  $K_e$ , to quantify the individual contributions for the two components of  $ET_c$ . The dual procedures also include a water stress coefficient ( $K_s$ ) to quantify the effects of soil water stress on  $ET_c$ . Several recent studies conducted in Texas and Arizona have shown that the FAO-56 dual crop coefficient procedures can provide good estimates of daily  $ET_c$  for fully-irrigated grain sorghum (Tolk and Howell 2001), cotton (Hunsaker 1999; Howell et al. 2002), and alfalfa (Hunsaker et al. 2003).

While the FAO-56 dual procedures provide an excellent framework for calculating daily  $ET_c$ , its successful application in providing reliable estimates for irrigation scheduling is highly dependent on the ability to construct a  $K_{cb}$  curve that matches the actual crop growth conditions that occur during a given season (Allen et al. 1998; Hunsaker et al. 2003). Because the  $K_{cb}$  curve functions described in FAO-56, and generally those used with most state-of-the-art irrigation-scheduling programs, are time-based, they lack the flexibility required to capture atypical crop development and water-use patterns caused by weather anomalies (Bausch and Neale 1989). Some improvements over time-based curves to account for the effects of climatic variability have been reported when  $K_{cb}$  curves were derived as a function of a thermal-based index, such as cumulative growing-degree-days (GDD) (Stegman 1988; Slack et al. 1996).

The  $K_{cb}$  curve is designed to reflect  $ET_c$  for optimum agronomic and water management conditions (Allen et al. 1998). However,  $K_{cb}$  curve adjustment to estimate  $ET_c$  when crop growth and water use deviate from "standard" conditions due to nutrient, crop density, pest, or other crop stress factors are not commonly nor easily implemented using conventional  $K_{cb}$  curves. Appropriate irrigation scheduling is also hindered by occurrences of spatially and temporally variable  $ET_c$  fluxes within a field or area created by a variety of factors, for example, non-uniform water application, soil water-holding characteristics, nutrient availability, stand density, and micro-climatic conditions. However, accounting for spatial and temporal variations in water use with present crop coefficient procedures is extremely difficult, if not impossible. Even for standard agronomic, water management, and weather conditions, and minimal crop variability, applying crop coefficient curves from the literature will usually require some form of locality adjustment, unless the curves were specifically developed for the particular location.

Remote sensing techniques offer a means of overcoming many of the shortcomings of conventional crop coefficient  $ET_c$  estimation by providing real-time feedback on daily crop water use as influenced by actual crop developmental patterns, local atmospheric conditions,

and field spatial variability. Multispectral vegetation indices (VIs), computed as differences, ratios, or linear combinations of reflected light in the visible (blue, green, or red) and near infrared (NIR) spectra have been found to be closely related to several crop growth parameters (Heilman et al. 1982; Jackson and Huete 1992; Moran et al. 1995). The simple ratio (NIR/red) and the normalized difference vegetation index [ $NDVI = (NIR - red)/(NIR + red)$ ] have gained wide acceptance for estimating plant cover, green plant biomass, and leaf area index. The potential to use multispectral VIs as near real-time surrogates for crop coefficients was proposed over two decades ago by Jackson et al. (1980), who pointed out the similarity between the seasonal pattern of a VI for wheat and that of the wheat crop coefficient. This VI-based crop coefficient concept was established by Bausch and Neale (1987) and Neale et al. (1989) who derived basal crop coefficients for corn in Colorado based on several VIs. Bausch and Neale (1989) and Bausch (1995) incorporated VI-based corn coefficients for use in existing scheduling algorithms and reported improvements in corn irrigation scheduling due to better estimation of water use and more appropriate timing of irrigations. Implementing VI-based crop coefficients within irrigation scheduling procedures could potentially be more successful and far-reaching than other remote sensing methods, because of the widespread familiarity and use of the crop coefficient methodology. In addition, VI data can be routinely measured either on the ground, in the air, or by satellite. Determining daily crop ET with the VI-based crop coefficient would require frequent, but not daily, VI measurements, since the smooth general shape of the  $K_{cb}$  curve over a growing season would allow data to be extrapolated over a period of up to a week. Only limited research has been conducted to expand the development of VI-based crop coefficients for crops other than corn, although simulation studies suggest that VIs could be used to obtain crop coefficients for several other important agricultural crops (Choudhury et al. 1994).

Cotton (*Gossypium hirsutum* L.) is one of several primary crops produced in the arid, desert regions of the southwestern USA. Cotton's high water-use requirement coupled with increasing costs for water in the region require cotton growers to implement irrigation practices that will lead to increased water-use efficiency. One of the most important elements will be a greater emphasis on proper irrigation scheduling. The focus of this article is to provide a means to improve cotton irrigation scheduling via real-time crop coefficient  $ET_c$  estimation.

Data on  $ET_c$  obtained for two cotton seasons during previous experiments in the southwestern USA were used to derive basal crop coefficient data using back-calculations of the FAO-56 dual crop coefficient procedures. The objectives were to develop a model based on the derived data for estimating  $K_{cb}$  for a full-season cotton crop as a function of the multispectral vegetation index, NDVI; and to provide an initial performance

evaluation of the model based on field data for another full-season cotton cultivar grown in a different year.

## Methods and materials

Data acquired during Free-Air CO<sub>2</sub> Enrichment (FACE) cotton experiments in 1990 and 1991 were used to derive cotton basal crop coefficients for developing an NDVI-based  $K_{cb}$  model. The FACE studies were conducted on production-scale cotton fields in central Arizona (Hendrey and Kimball 1994), during which data were collected for a wide range of plant, soil, and meteorological parameters. Information about the experimental procedures, and various descriptions on the methodology of data collection and interpretation, are provided in Mauney et al. (1994), Hunsaker et al. (1994), and Pinter et al. (1994, 1996).

The broad objective for the FACE experiments was to study the interactive effects of elevated CO<sub>2</sub> and irrigation water supply on cotton. Experimental treatments included cotton grown under both ambient CO<sub>2</sub> (control treatment) and at concentrations about 45% higher than ambient (FACE treatment) with ample (wet treatment) and limited (dry treatment) water application. However, the data used in the derivation of the cotton basal crop coefficients excluded treatments exposed to either elevated CO<sub>2</sub> or limited water application. Therefore, only the control-wet (CW) treatment data were used. Brief descriptions of the experimental methodology and specific measurements pertinent to the present study follow.

### Crop culture

Experiments were conducted during 1990 and 1991 on a 9-ha field at the University of Arizona, Maricopa Agricultural Center (MAC). A full-season, short-staple cotton (*Gossypium hirsutum* L., cv. Deltapine 77), well-adapted to central Arizona climatic conditions, was seeded during mid- to late April in east-west rows on raised soil beds, spaced 1.02 m apart. After emergence, the population was thinned to 10 plants m<sup>-2</sup>. Cultivation, insect and weed control, and nutrient application were managed according to recommendations of the Arizona State Extension Service and University of Arizona research and support staff. Cotton was supplied with an average of 142 kg ha<sup>-1</sup> N during each year (Pinter et al. 1996). Irrigation was terminated and seed cotton was harvested in mid-September of each year.

### Soil characteristics

The soil at the FACE experimental site is classified as a Trix clay loam [fine-loamy, mixed (calcareous), hyperthermic Typic Torrifluents]. Volumetric soil water contents for the top 0.7 m of the soil profile average 30 and 20% at soil matric potentials of -33 and -1,500 kPa, respectively, whereas the corresponding water contents for the subsurface profile (0.7–2.0 m) average 22 and 12%, respectively (Hunsaker et al. 1994).

### Irrigation management

Irrigation water was supplied with a subsurface drip irrigation system that included a single micro-tube line per 1.02-m row, buried 0.18–0.25 m below the soil surface. Irrigation timing and amounts for “wet” irrigation treatments were determined using estimates of cotton ET<sub>c</sub> based on cotton crop coefficients multiplied by reference evapotranspiration (Mauney et al. 1994). Three days after planting, 290 and 270 mm of water was applied to all treatments for seed germination in 1990 and 1991, respectively (Hunsaker et al. 1994). Cumulative amounts of the metered irrigation applications from planting through harvest averaged 1,180 and 1,030 mm for the CW treatments of 1990 and 1991,

respectively, and seasonal rainfall was 125 and 41 mm in 1990 and 1991, respectively (Hunsaker et al. 1994).

### Crop height and leaf area index measurements

Cotton canopy height ( $h_c$ ) and leaf area index (LAI) were measured at 7- to 14-day intervals during the growing season (Mauney et al. 1994). Thirteen measurements were made in 1990 and 16 in 1991.

### Evapotranspiration from soil water balance

Soil water contents were measured at two locations in each plot with neutron-scattering equipment at 7- to 14-day intervals during the two cotton growing seasons (Hunsaker et al. 1994). Measurements were made during early morning hours. Residuals calculated from the soil water-balance equation (Jensen et al. 1990) were used to determine the cumulative cotton ET<sub>c</sub> that occurred between successive soil water content measurements, assuming negligible drainage below the crop root zone.

### Meteorological data and reference evapotranspiration (ET<sub>o</sub>)

Meteorological data were provided by an AZMET weather station (Brown 1989) located on a well-watered grass site at MAC ~2 km from the field site. Daily AZMET data for solar radiation, air temperature, wind speed, and humidity were used to calculate daily grass-reference evapotranspiration (ET<sub>o</sub>) using the FAO Penman–Monteith method [equation 6 in FAO-56 (Allen et al. 1998)]. The AZMET weather station also provided information on daily cotton heat units, or growing-degree-days (GDD), which were calculated by the sine curve method using upper and lower air temperature thresholds of 30 and 12.8°C, respectively, as described by Brown (1991).

### Canopy reflectance and transmittance

Crop canopy reflectance factors were measured two to four times a week during the growing seasons (Pinter et al. 1994). In 1990, 44 sets of canopy reflectance measurements were made between 30 April and 18 September, and in 1991, 70 sets of measurements were made between 19 April and 15 September. Observations were made for all plots using a hand-held, four-band radiometer equipped with 15° field-of-view optics and spectral bandpass spanning three visible (blue, green, and red) and one NIR wavelength intervals. Data were collected at a morning time period corresponding to a nominal solar zenith angle of 45°. The NDVI was computed from reflectance factors in near infrared (0.79–0.89 μm) and red (0.61–0.68 μm) wavebands as:  $NDVI = (NIR - red) / (NIR + red)$ .

Pinter et al. (1994) also described measurements of the incident, transmitted, and reflected components of the radiation balance using a single, hand-held, line quantum sensor. They computed the fraction of the photosynthetically active radiation (PAR) absorbed by the canopy ( $f_{APAR}$ ) from a light balance equation using the measured fractions of PAR transmitted through the canopy ( $f_{TPAR}$ ), reflected from the canopy, and reflected from the soil. The data were obtained on three dates in 1990 and seven dates in 1991 for all plots. In both years, the initial line quantum sensor measurements were begun 49 days after crop emergence.

### Basal crop coefficient derivation: general methodology

The FAO-56 dual crop coefficient approach (Allen et al. 1998) describes the relationship between ET<sub>c</sub> and ET<sub>o</sub> by separating the single  $K_c$  into the basal crop and soil water evaporation coefficients:

$$K_c = (K_{cb} + K_e) = ET_c / ET_o \quad (1)$$

where  $ET_c$  and  $ET_o$  are in  $\text{mm day}^{-1}$ .

The basal crop coefficient,  $K_{cb}$ , represents the ratio of  $ET_c/ET_o$  for conditions when, first, the soil surface layer is dry (i.e., when  $K_e = 0$ ) and, second, the soil water within the root zone is adequate to sustain full plant transpiration (non-stressed conditions). The soil evaporation coefficient,  $K_e$ , describes the contribution of the evaporation component of  $ET_c$  when the soil surface is wetted following irrigation or rain (Allen et al. 1998). When the available soil water of the root zone drops below a critical level, crop water stress can occur and reduce  $ET_c$ . In the FAO-56 dual procedures, the effects of water stress on  $ET_c$  can be estimated by multiplying  $K_{cb}$  by the water stress coefficient ( $K_s$ ):

$$K_{cb}K_s + K_e = ET_c / ET_o \quad (2)$$

where  $K_s < 1$  when the available soil water is insufficient for full  $ET_c$ , and  $K_s = 1$  when there is no soil water limitation on  $ET_c$ .

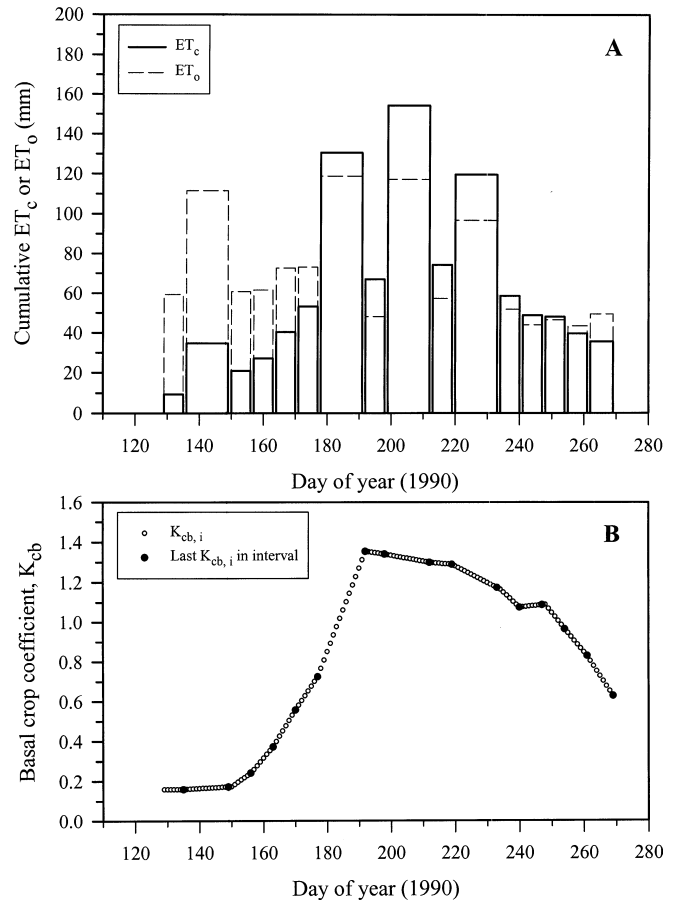
Soil water-balance determinations of cotton cumulative  $ET_c$  for 7- to 14-day intervals during the cotton growing seasons were applied in back-calculations of the FAO-56 dual crop coefficient procedures to derive daily  $K_{cb}$  data for the entire growing season. The approach was similar to back-calculations of the FAO-56 procedures for deriving alfalfa  $K_{cb}$  from  $ET_c$  measurements (Hunsaker et al. 2003). The  $K_{cb}$  data were derived separately for each of the four control-wet replicates in both the 1990 and 1991 FACE experiments. Cumulative  $ET_c$  determinations for each measurement interval during the 1990 season are shown for replicate 1 of the CW treatment in Fig. 1a, along with the cumulative  $ET_o$  for each interval.

For each replicate, daily time-step calculations for  $K_{cb}$ ,  $K_e$ ,  $K_s$ ,  $ET_c$ ,  $ET_o$ , and other parameters (described later) required in the FAO-56 dual crop coefficient procedures were made within a spreadsheet that contained all the computations for each day of the growing season. The days for the growing season were then partitioned into a series of successive time intervals, whose lengths (7 to 14 days) were established by the number of days between two successive soil water content measurements. For each 7- to 14-day interval, the cumulative  $ET_c$  for the interval was known from soil water-balance measurements and the daily  $ET_o$  for each day in the interval was calculated from the FAO Penman-Monteith equation using daily weather data. Thus, for a given interval, the daily values for  $K_{cb}$ ,  $K_e$ , and  $K_s$  were determined as a consequence of the known values for cumulative  $ET_c$ , daily  $ET_o$ , and other parameter estimates, using back-calculations of the dual crop coefficient calculations. This can be described mathematically for a given interval from day 1 to day  $n-1$ , as:

$$ET_{c,i} = (K_{cb,i}K_{s,i} + K_{e,i})ET_{o,i} \quad (3)$$

where day 1 is the day a soil water content measurement was made, and day  $n$  is the next day a soil water content measurement was made; the summation of  $ET_{c,i}$  from day 1 to day  $n-1$  equals the cumulative  $ET_c$  for the interval;  $K_{cb,i}$ ,  $K_{s,i}$ , and  $K_{e,i}$  are the basal crop, water stress, and soil evaporation coefficients on day  $i$ , respectively; and  $ET_{o,i}$  is the grass-reference evapotranspiration on day  $i$ .

Derivation involved adjusting the  $K_{cb,i}$  values for the given measurement interval until the right-hand side of Eq. 3 matched the quantity on the left-hand side of the equation, i.e., the actual cumulative  $ET_c$  that was determined for the interval. However, for each measurement interval, the  $K_{cb,i}$  values were forced to either increase or decrease linearly along the same slope from the first to the last day of the interval, with  $K_{cb}$  magnitude dependent upon the value for the  $K_{cb,i}$  determined on the last day of the previous measurement interval. This is illustrated with the  $K_{cb,i}$  data derived for replicate 1 of the CW treatment in 1990 (Fig. 1b), which shows that the  $K_{cb,i}$  for this replicate increased from interval to interval (positive slopes) during the first half of the growing season, and typically decreased (negative slopes) during the second half of the season.

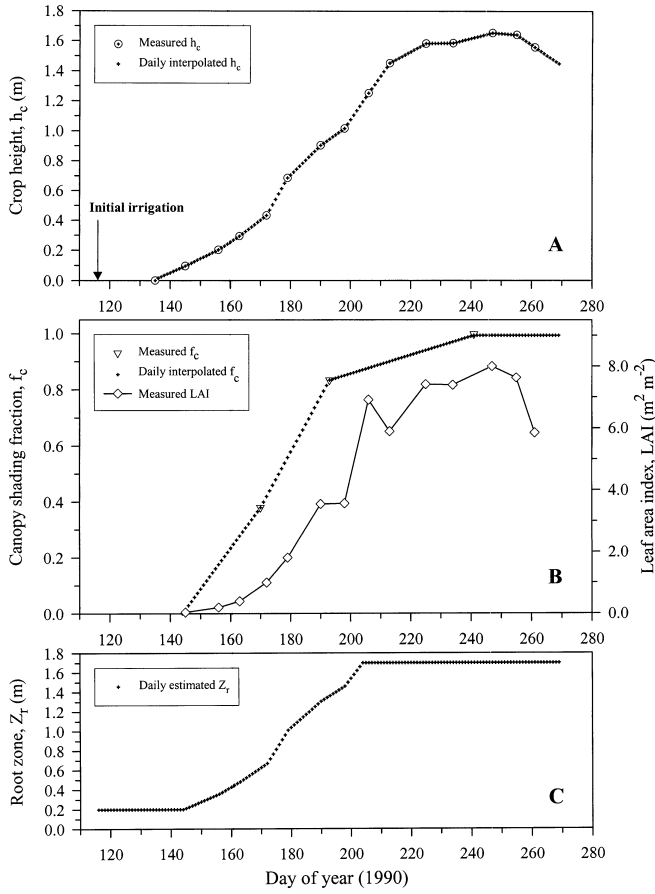


**Fig. 1 a** Cumulative  $ET_c$  determinations for 7–14 day measurement intervals for replicate 1 of the control-wet (CW) treatment during the 1990 FACE experiment, along with the calculated cumulative  $ET_o$  for each interval; **b** derived daily  $K_{cb}$  with indication of the daily  $K_{cb}$  value at the end of each measurement interval

#### Calculation of $K_e$

The FAO-56 dual crop coefficient calculations were used to estimate the separate contribution to  $ET_c$  apart from basal crop water use, due to soil evaporation (described by  $K_e$ ) following surface soil wetting from irrigation and rainfall. Daily values for  $K_e$  are determined using a daily soil water-balance computation of the surface soil evaporation layer ( $Z_e$ ) subject to drying by evaporation. Soil parameters required to determine daily  $K_e$  include the field capacity (FC) and permanent wilting point (PWP) of the surface soil layer, the readily evaporable water (REW), and the depth of  $Z_e$ . The same soil parameters were used for all replicates in both years. The FC and PWP were taken as the site-average volumetric soil water contents in the upper profile at soil matric potentials of  $-33$  and  $-1,500$  kPa, respectively. A typical REW value for a loam soil of 10 mm (FAO-56, table 19) and a surface soil evaporation layer,  $Z_e$ , of 0.125 m were used in the calculations. The total evaporable water (TEW) of the soil surface layer, calculated using FAO-56, equation 73, was 25 mm. Daily values for crop height,  $h_c$ , used in the FAO-56  $K_e$  calculations, were estimated by linear interpolation of the measured crop heights, as illustrated in Fig. 2a for replicate 1 of the CW treatment of 1990.

Two final parameters are required for determining  $K_e$ : (1) the daily fraction of the soil surface shaded by the canopy ( $f_c$ ), or conversely the unshaded fraction ( $1-f_c$ ), and (2) the fraction of the soil surface wetted ( $f_w$ ) during each irrigation and precipitation event. Values for the unshaded fraction of the canopy,  $1-f_c$ , were



**Fig. 2** For replicate 1 of the CW treatment, 1990 FACE experiment: **a** measured and interpolated crop height ( $h_c$ ); **b** measured and interpolated canopy shading fraction ( $f_c$ ) and measured leaf area index ( $LAI$ ); **c** estimated depth of daily root zone ( $Z_r$ )

approximated from the fraction of the incident PAR transmitted through the canopy, as determined from line quantum sensor measurements. Daily values for  $f_{TPAR}$  ( $\approx 1 - f_c$ ) were estimated by linear interpolation between days of measurement. The interpolated measured data for canopy shading fraction ( $f_c$ ) and measured LAI data followed similar trends throughout the growing season (Fig. 2b). For both years and all replicates, a value of 1.0 was assigned for  $f_w$  when rain occurred (i.e., the entire soil surface was assumed to have been wetted). Following subsurface drip irrigation events, the value used for  $f_w$  was calculated using the FAO-56 recommendations for subsurface drip systems as follows:

$$f_w = 0.30(1 - 0.67f_c) \quad (4)$$

#### Calculation of $K_s$

A daily soil water balance of the active root zone (separate from the surface soil evaporation layer soil water balance) is needed in the FAO-56 calculations to determine the daily water stress coefficient,  $K_s$ , and thereby any reduction for daily  $ET_c$  due to soil water stress. The root zone water-balance equation (FAO-56, equation 85) expresses soil water contents in terms of root zone depletion ( $D_r$ ). Thus,  $D_r$  is viewed as the depth of water required to refill the root zone to field capacity. The root zone water balance for an interval from day  $i$  to day  $i+1$  is written as:

$$D_{r,i+1} = D_{r,i} + R_i + I_i - ET_{c,i} - DP_i \quad (5)$$

where

- $D_{r,i}$  root zone depletion at the beginning of day  $i$  (mm),
- $D_{r,i+1}$  root zone depletion at the beginning of the next day  $i+1$  (mm),
- $R_i$  rainfall during day  $i$  (mm),
- $I_i$  irrigation depth during day  $i$  (mm),
- $ET_{c,i}$  crop evapotranspiration for day  $i$  (mm),
- $DP_i$  deep percolation out of the root zone on day  $i$  (mm)

The FAO-56 root zone water balance limits the minimum value of  $D_r$  to zero (i.e., field capacity). In the absence of irrigation or rainfall, calculation of equation 5 results in an increase in the root zone depletion at the beginning of day  $i+1$  due to  $ET_{c,i}$ . Following irrigation or rain on day  $i$ , the root zone water balance (when assuming deep percolation is zero) may calculate an increase in  $D_{r,i+1}$  that exceeds FC (i.e., results in a negative value for  $D_{r,i+1}$ ). When this occurred, the total amount of water above field capacity on day  $i+1$  was assumed to have been lost to deep percolation on day  $i$ , following any  $ET_c$  for day  $i$ .

In the FAO-56 procedures,  $K_s$  is described as a function of the total available water (TAW) within the root zone, the readily available water (RAW) within the root zone, and  $D_r$ , as determined from the root zone water balance. For a given day  $i$ , the calculation of  $K_s$  is given as:

$$K_{s,i} = (TAW_i - D_{r,i}) / (TAW_i - RAW_i) \quad (6)$$

where  $K_{s,i} = 1$  when  $D_{r,i}$  is smaller than or equal to  $RAW_i$ , and  $K_{s,i} < 1$  otherwise. For a given day,  $TAW_i$  is determined from the daily crop rooting depth ( $Z_{r,i}$ ) and the FC and PWP for soil at the rooting depth. The  $RAW_i$  is then expressed as  $pTAW_i$ , where  $p$  is the soil depletion factor that represents the fraction of TAW that can be depleted from the root zone before water-stress occurs.

In computing daily  $K_s$  with Eq. 6, it was assumed that the daily  $Z_r$  for all replicates of both years increased from a minimum value of 0.20 m for the first 30 days of the season to a maximum of 1.7 m at mid-season (Allen et al. 1998), and that the development of  $Z_r$  increased in proportion to the increase in the measured and interpolated crop height. As shown for replicate 1 of the CW treatment in 1990, the maximum  $Z_r$  (Fig. 2c) was presumed to be reached when crop height had increased to 1.2 m on day of year (DOY) 204 (Fig. 2a).

The recommended  $p$  value for cotton when  $ET_c$  is  $5 \text{ mm day}^{-1}$  is 0.65 (FAO-56, table 22). Following FAO-56 procedures,  $p$  was adjusted when  $ET_c$  differed from  $5 \text{ mm day}^{-1}$  by the FAO-56 numerical approximation:

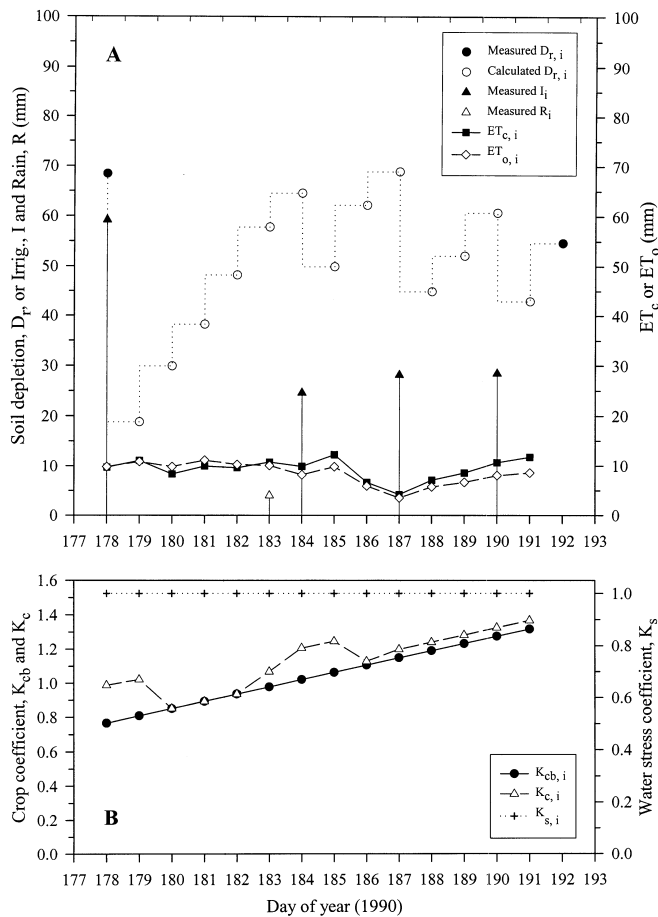
$$p_i = 0.65 + 0.04(5 - ET_{c,i}) \quad (7)$$

where  $p_i$  is the soil depletion fraction on day  $i$ , limited to  $0.1 \leq p_i \leq 0.8$ , and  $ET_{c,i}$  is the cotton  $ET_c$  on day  $i$ , in  $\text{mm day}^{-1}$ .

#### Example of back-calculations and $K_{cb}$ derivation

Daily  $K_{cb}$  values derived using the FAO-56 back-calculations are illustrated for a 14-day measurement period (DOY 178–191) for replicate 1 in 1990 (Fig. 3). The measured cumulative  $ET_c$  was 131 mm and the cumulative  $ET_o$  was 119 mm from DOY 178–191. Root zone water-balance computations (Eq. 5) for each day of the interval began with the measured  $D_r$  made at the beginning of DOY 178 (shown as an enclosed circle in Fig. 3a). The open circles are the computed  $D_r$  at the beginning of each subsequent day in the interval, as determined after the appropriate irrigation and rain additions and  $ET_c$  subtractions are calculated from the root zone water balance for the previous day. For this example, and for the vast majority of intervals, daily root zone water-balance calculations suggested that no water was lost to deep percolation during the interval.

For  $K_{cb}$  derivation, the daily root zone computations for each measurement interval are forced to satisfy the condition that the computed and measured  $D_r$  be identical at the beginning of the next measurement interval (which occurred on DOY 192 for this



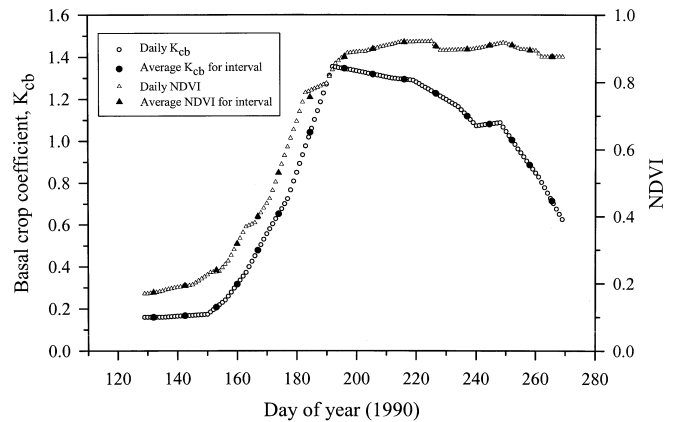
**Fig. 3** For replicate 1 of the CW treatment, 1990 FACE experiment: **a** daily root zone water balance (Eq. 5) components for the measurement interval from DOY 178 to DOY 191 showing measured and calculated daily root zone depletion ( $D_{r,i}$ ), daily measured irrigation ( $I_i$ ) and rainfall ( $R_i$ ), daily estimated evapotranspiration ( $ET_c$ ), and calculated reference evapotranspiration ( $ET_o$ ); **b** estimated daily basal crop coefficient ( $K_{cb,i}$ ), estimated total daily crop coefficient ( $K_{c,i}$ ), and estimated daily water stress coefficient ( $K_{s,i}$ ) for days in the measurement interval

example). This condition implies that the summation of the computed daily  $ET_c$  from Eq. 3 (dependent upon daily  $K_{cb}$ ) be identical to the measured cumulative  $ET_c$  for the interval. As the daily  $K_{cb}$  curve for the interval is adjusted, FAO-56 procedures calculate new estimates for daily  $ET_c$ , and the daily root zone computations are accordingly updated. Computations for the interval end when adjustment results in derived daily  $K_{cb}$  data that satisfy the root zone water-balance condition.

For the example interval, the daily root zone depletion computations applied in FAO-56 procedures indicated that water stress did not occur ( $K_s = 1$ ) for any day (Fig. 3b). The difference between the  $K_c$  and  $K_{cb}$  value for a given day describes the magnitude for  $K_e$ , and thus the estimated contribution of soil evaporation for  $ET_c$  on the day. The daily  $K_e$  were increased following irrigation and rain, but the magnitudes for  $K_e$  decreased as  $K_{cb}$  (as well as canopy shading) increased during the interval (Fig. 3b).

#### Paired NDVI observations with derived $K_{cb}$

The measured NDVI for each control-wet replicate were interpolated linearly, generating daily NDVI values for the entire season. For each replicate, the average daily NDVI was calculated for each 7- to 14-day measurement interval during the season. The average



**Fig. 4** Daily  $K_{cb}$  and normalized-difference vegetation index (NDVI) for replicate 1 of the CW treatment, 1990 FACE experiment, with indication of the average  $K_{cb}$  and NDVI (data pairs) as referenced by the mid-day for each of the measurement intervals

daily values were then paired with derived average daily  $K_{cb}$  values obtained for the corresponding replicate and measurement interval. The time-reference for the paired NDVI- $K_{cb}$  data was taken as the middle day of the particular measurement interval. An example of the interval NDVI and  $K_{cb}$  data pairs obtained for replicate 1 of the CW treatment in 1990 is shown (Fig. 4). Regression procedures were used to model the NDVI- $K_{cb}$  relationship using data for all replicates and both years.

#### Evaluation data

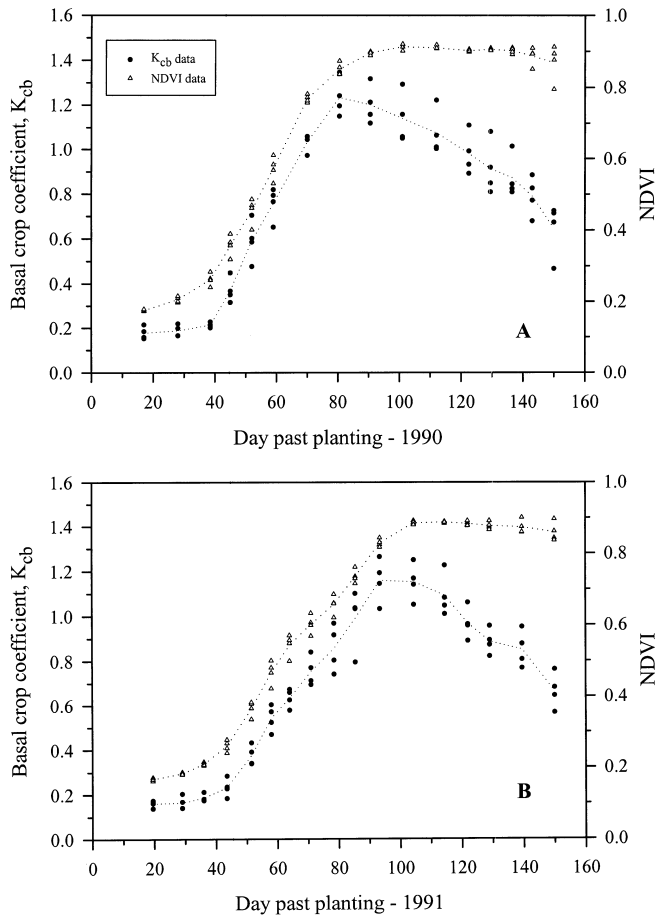
The NDVI- $K_{cb}$  model was evaluated using data for another full-season cotton cultivar (*Gossypium hirsutum* L., cv. Deltapine 90) grown in another year, 1998, on a 1.3-ha sandy loam site at MAC. As described by Colaizzi et al. (2003), the experiment, initiated in late April 1998, consisted of two nitrogen levels with 16 treatment plots, with each plot  $\sim 22 \times 22$  m in size. The cotton was surface irrigated, and grown in the same row orientation (east-west) as the cotton in the FACE experiments. Soil water-content measurements using neutron probe and time domain reflectometry (Colaizzi et al. 2003) were begun in late May 1998. Supporting measurements collected during the experiment included canopy reflectances (NDVI) taken three times per week for each plot using a hand-held radiometer and, on a weekly basis, biomass, leaf area, plant height, and percentage canopy cover.

Two particular treatment plots (ample-N treatment) from the 1998 experiment that were described by Colaizzi et al. (2003) were used in this study for evaluating the NDVI-based model. Soil water-content data for each plot were used to calculate the cumulative  $ET_c$  for measurement intervals during the growing season, as was done for the FACE cotton replicates. Next, daily  $K_{cb}$  for the plots were derived using the previously described back-calculations of the FAO-56 dual procedures. Finally, estimated  $ET_c$  was calculated using the FAO-56 procedures with daily  $K_{cb}$  values generated from the model regression equations and measured NDVI data. Measured crop and soil parameters for the 1998 plots and local AZMET weather station data were used in the  $K_{cb}$  back-calculations and FAO-56  $ET_c$  estimation procedures.

## Results and discussion

### NDVI- $K_{cb}$ model

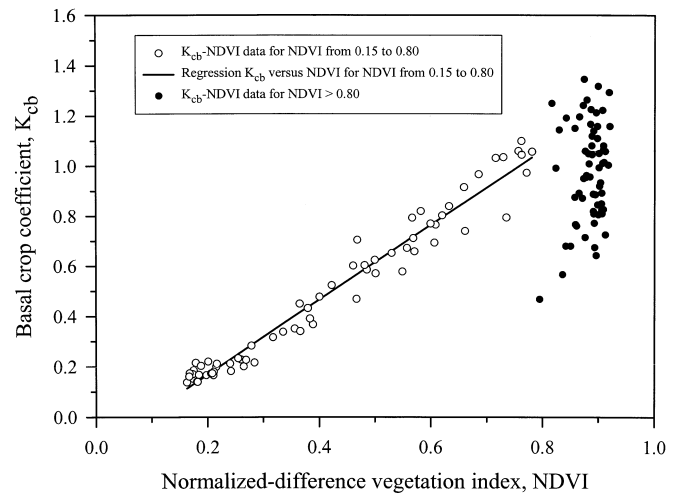
Values for  $K_{cb}$  and NDVI plotted versus days past planting reveal that both parameters increased in a



**Fig. 5** Paired  $K_{cb}$  and normalized-difference vegetation index (NDVI) data with days past planting for all four replicates of control-wet treatment for **a** the 1990 and **b** the 1991 FACE experiments

similar manner from early crop development until a maximum  $K_{cb}$  was attained (Fig. 5a, b). For both years, maximum  $K_{cb}$  occurred at just about the time of effective canopy closure, when NDVI values for replicates were on the order of 0.80 or above, ~81 and 94 days after planting for the 1990 (Fig. 5a) and 1991 (Fig. 5b) cotton-growing seasons, respectively. After effective full cover, NDVI vacillated within only a narrow range between 0.85 and 0.92 until about 140 days past planting. Thereafter, the NDVI for some replicates decreased below 0.85, indicating the beginning of crop senescence. Unlike the horizontal trend which occurred for NDVI after full cover, values for  $K_{cb}$  began to decrease with time once maximum  $K_{cb}$  had been attained. Consequently, to adequately describe the change in  $K_{cb}$  during the entire growing season, the NDVI-based  $K_{cb}$  model was developed using two separate regression functions that intersect approximately when effective full cover is reached.

The first relationship (open circles in Fig. 6) is a linear regression function that describes the increase in  $K_{cb}$  with NDVI from initial crop growth (NDVI ≈ 0.15) through the beginning of full cover, using an upper



**Fig. 6** Plotted  $K_{cb}$  versus normalized-difference vegetation index (NDVI) for  $K_{cb}$ -NDVI data pairs from all four replicates of the CW treatments of 1990 and 1991, and linear regression line for  $K_{cb}$  as a function of NDVI. Data pairs for NDVI greater than 0.80 were excluded from the regression

bound of 0.80 for NDVI. Linear regression of  $K_{cb}$  with NDVI using data for all replicates and both years resulted in an  $r^2$  of 0.97, with minimal scatter around the regression line. Resultant regression coefficients and statistics are presented in Table 1. The  $K_{cb}$ -NDVI pairs shown when the NDVI increased above 0.80 (closed circles in Fig. 6) illustrate the deviation of the data from the linear function shortly after effective full cover was attained.

The pronounced downward trend for  $K_{cb}$  with minimal corresponding decreases for NDVI after full cover suggested that a time-dependency parameter added within the NDVI index would significantly improve  $K_{cb}$  estimation during the latter part of the growing season. Although several regression function forms and time-based indices were considered, a simple multiple linear regression function (Table 1) with cumulative GDD for the time index and NDVI for the crop growth index was selected for modeling the observed  $K_{cb}$  after full canopy was attained (Fig. 7a). For this relationship, growing-degree-days were accumulated, starting on the day NDVI reached 0.80 for a given replicate. Assuming constant NDVI values of 0.85 and 0.90 after full cover,  $K_{cb}$  generated with the multiple regression function illustrate how a relatively small difference in NDVI would affect the estimated magnitude of  $K_{cb}$  during the latter part of the growing season (Fig. 7b).

#### Evaluation of NDVI-based $K_{cb}$ model

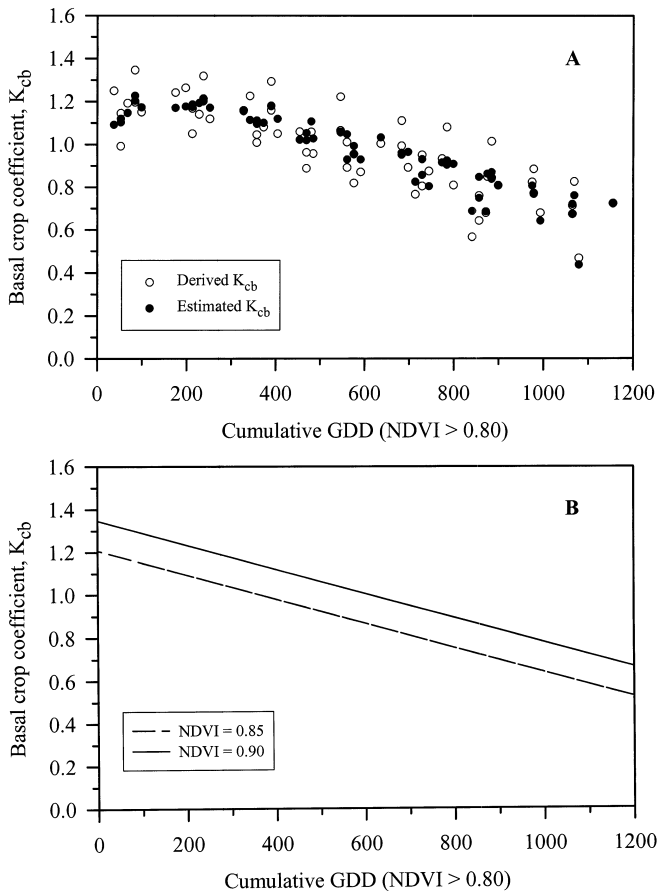
Evaluation of the NDVI-based  $K_{cb}$  model was made using data for two plots within the ample-N treatment of the 1998 cotton field experiment (Colaizzi et al. 2003). The derived daily  $K_{cb}$  for the replicates are compared with daily  $K_{cb}$  estimated from the model

**Table 1** Regression coefficients and statistics relating cotton  $K_{cb}$  to normalized-difference vegetation index (NDVI) and cumulative growing-degree-days (GDD)

Growth stage	NDVI range	Regression coefficients			Regression statistics <sup>a</sup>		
		NDVI	Cumulative GDD <sup>b</sup>	Intercept	$r^2$	SE ( $K_{cb}$ )	$n$
Early vegetative to effective full cover	0.15 to 0.80	1.49	na	-0.12	0.97	0.06	68
After effective full cover	> 0.80	2.80	$-5.69 \times 10^{-4}$	-1.17	0.82	0.09	64

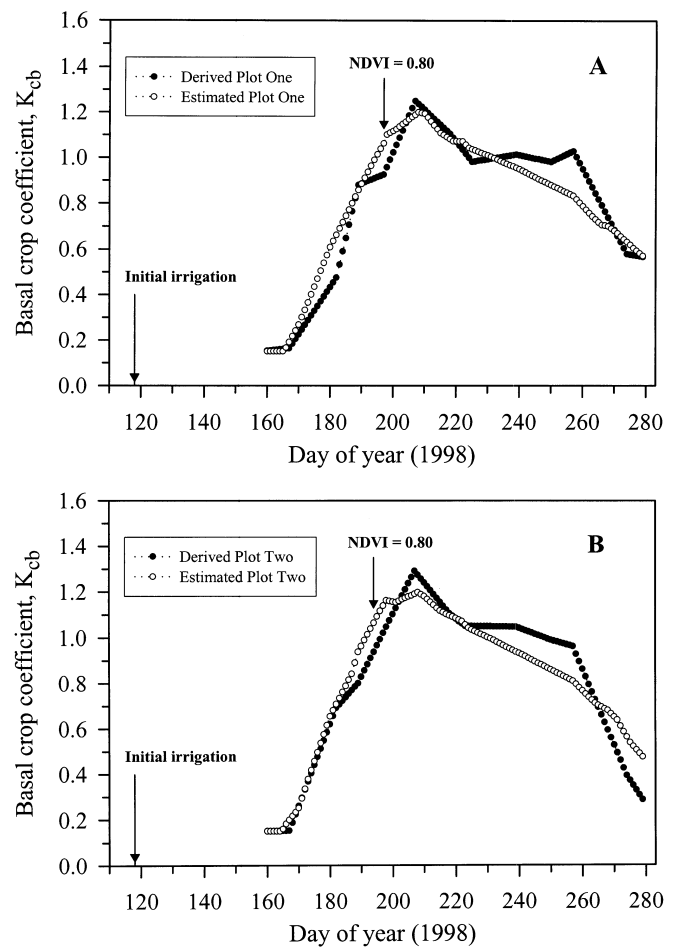
<sup>a</sup>  $r^2$  is the coefficient of determination, SE ( $K_{cb}$ ) is the standard error of the  $K_{cb}$  estimates, and  $n$  is the number of data points

<sup>b</sup> Accumulation of GDD start when NDVI = 0.80. Note GDD are calculated by the sine curve method using upper and lower temperature thresholds of 30 and 12.8°C, respectively



**Fig. 7** **a** One-dimensional plot of  $K_{cb}$  data for CW replicates of 1990 and 1991, when the corresponding normalized-difference vegetation index (NDVI) was greater than 0.80, shown as a function of cumulative growing-degree-days (GDD), and estimates for  $K_{cb}$  calculated as a function of NDVI and cumulative GDD using the multiple regression function given in Table 1; **b** hypothetical  $K_{cb}$  lines calculated from the multiple regression function versus cumulative GDD when assuming constant values of 0.85 and 0.90 for NDVI. Note that the accumulation of growing-degree-days begin when the NDVI first reaches 0.80

regression functions based on NDVI measurements (Fig. 8a, b). Note that the time NDVI first reached 0.80 ( $\approx$  effective full cover) for each plot is indicated in the figures, and marks the point at which the calibration transferred from the linear to the multiple regression function. Prior to NDVI reaching 0.80, there was a tendency for the linear model to overestimate derived



**Fig. 8** Comparison of derived daily  $K_{cb}$  based on soil water-content measurements and back-calculations of the FAO-56 procedures with estimated daily  $K_{cb}$  based on NDVI measurements and the regression functions of Table 1 for **a** plot 1 and **b** plot 2 of the 1998 cotton experiment

$K_{cb}$ , although agreement between estimated and derived  $K_{cb}$  was excellent for plot 2 through DOY 185. For both plots, the  $K_{cb}$  agreement was reasonably good during mid-season, i.e., from DOY 200 through DOY 230. However, the modeled  $K_{cb}$  based on NDVI underestimated derived  $K_{cb}$  during the following 30 days (DOY 230–260). The slower decline for the derived  $K_{cb}$  during that period in 1998 relative to the estimated NDVI-based  $K_{cb}$  may have resulted from an



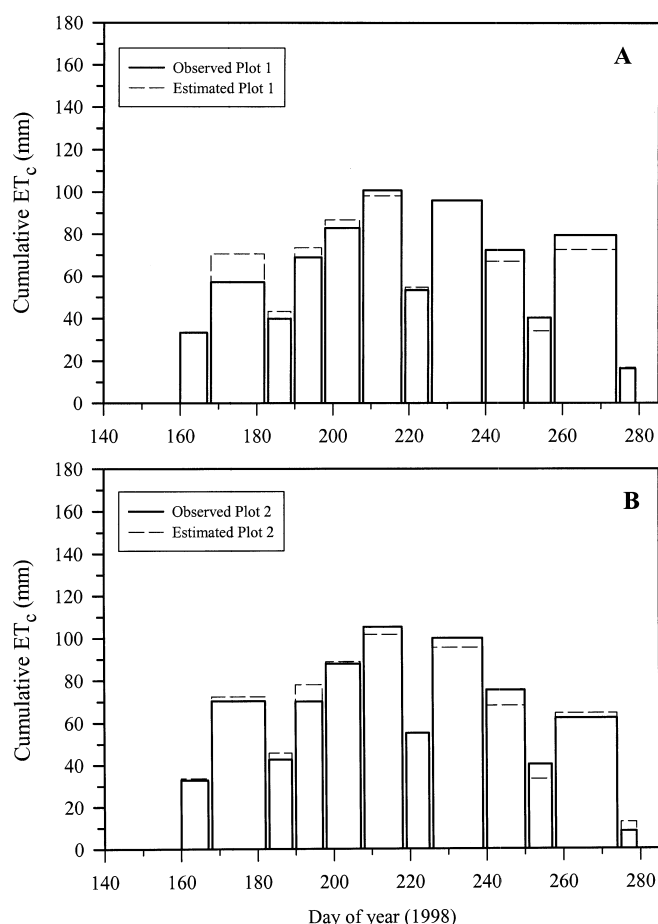
increase in the irrigation frequency to the 1998 plots starting on DOY 236 following installation and testing of a linear move irrigation system.

Cumulative  $ET_c$  estimated using the NDVI-based daily  $K_{cb}$  and FAO-56 dual crop coefficient procedures for the two plots of 1998 was in good agreement with observed cumulative  $ET_c$  based on soil water content data, as shown for 12 measurement periods occurring between DOY 160 and DOY 279 (Fig. 9a, b). As expected from the  $K_{cb}$  curves, the tendency was towards higher estimated  $ET_c$  than observed during the first half of the season prior to effective full cover, followed by lower estimated  $ET_c$  than observed for the latter half of the season. Considering all measurement periods for the first half of the season (DOY 160–207), estimated cumulative  $ET_c$  was 25 mm (9%) and 15 mm (5%) more than that observed for plots 1 and 2, respectively. For measurement periods from DOY 208 to DOY 279, estimated cumulative  $ET_c$  was 19 mm (4%) and 15 mm (4%) less than that observed for plots 1 and 2, respectively. Consequently, total estimated  $ET_c$  for all 12 measurement intervals differed

from the observed by only +6 mm and 0 mm for plots 1 and 2, respectively.

## Conclusions

Regression equations were developed to estimate the seasonal distribution of  $K_{cb}$  with the normalized-difference vegetation index for a full-season cotton cultivar grown in the southwestern USA. An initial evaluation of the model indicated that the NDVI-based  $K_{cb}$  provided  $ET_c$  estimations that closely described the observed  $ET_c$  attained for another cotton cultivar grown under different conditions than those under which the model was developed. The NDVI-based  $K_{cb}$  functions can be easily incorporated within the FAO-56 dual crop coefficient procedures and, thereby, provide a means to apply remotely sensed observations for real-time cotton irrigation scheduling. Additional experiments are currently being conducted in central Arizona to evaluate the NDVI-based  $K_{cb}$  application for use in scheduling irrigations for cotton. One area that will be addressed is the potential use of alternate vegetation indices or enhanced NDVI formulations to more readily track  $K_{cb}$  following canopy closure. Some of the primary benefits envisioned for using real-time multispectral-based  $K_{cb}$  in place of conventional  $K_{cb}$  curves include eliminating the need to hypothesize the time-scale for crop developmental stages and future weather conditions for a given cropping season. Because remotely sensed  $K_{cb}$  are expected to track the unique developmental patterns of the crop, field observation requirements, assumptions, and cumbersome procedures associated with adjusting conventional  $K_{cb}$  curves for conditions other than optimum could be eliminated as well. The remote sensing technique may also potentially provide the ability to detect and quantify differences in  $ET_c$  within a single field and on a field-by-field basis; information that at present is extremely difficult to obtain without labor-intensive methods.



**Fig. 9** Comparison of observed cumulative  $ET_c$  based on soil water-content measurements and estimated cumulative  $ET_c$  based on the modeled NDVI-based daily  $K_{cb}$  and FAO-56 dual crop coefficient calculations for a plot 1 and b plot 2 of the 1998 cotton experiment

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